

Diffusion

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1 Introduction

Diffusion controls a wide variety of processes and properties, including manufacturing of semiconductor devices, environmental degradation of structural materials, corrosion, and permeability in polymers. The *MedeA Diffusion* module enhances your calculations by automatically computing the diffusivity of selected species using atomistic molecular dynamics techniques, and facilitates observation of the diffusive behavior of the different components.

Key Benefits

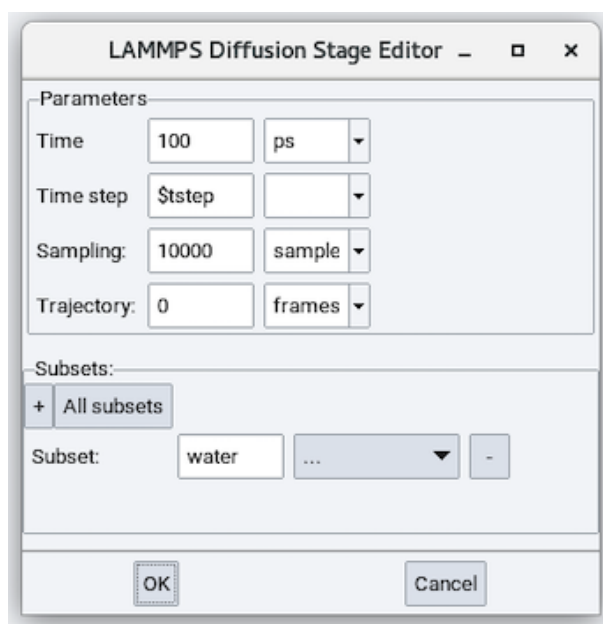
- Automated plot creation facilitates analysis of calculation results
- Visualization and confirmation of the presence of the diffusive dynamics regime through the provision of log(MSD) versus log(t) plots
- Calculation of the mean square displacement (MSD) of selected atom sets
- Determination of diffusion coefficients based on the Einstein diffusion equation
- Evaluation of calculation uncertainties

Hint: The *MedeA Diffusion* module works with classical molecular dynamics simulations using LAMMPS. Ab initio MD trajectories are not supported with the *Diffusion* module.

2 The *MedeA Diffusion* module

The *MedeA Diffusion* module can be accessed in a LAMMPS flowchart and you can insert the *Diffusion* stage into any LAMMPS simulation. The MSD of selected atoms is computed from simulation in the microcanonical (NVE) ensemble. LAMMPS molecular dynamics and automated analysis of simulation results complete the workflow.

The following illustrates the *MedeA Diffusion* stage:

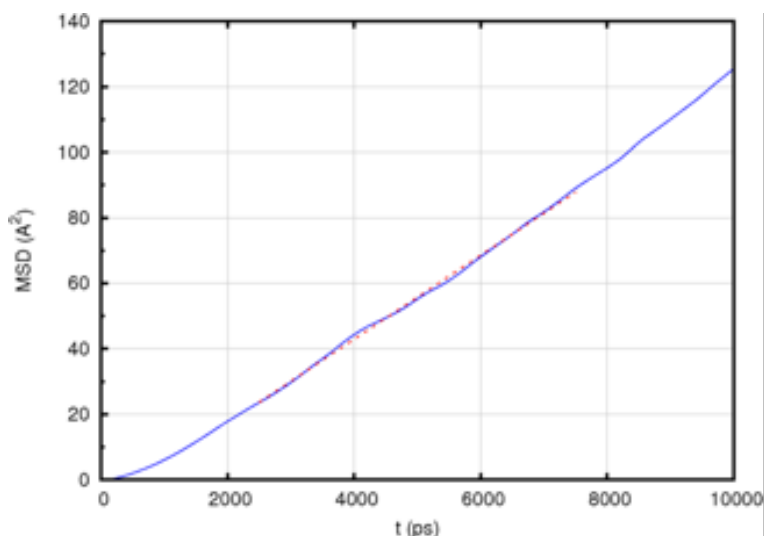


The parameters are:

- *Time*: Duration of the simulation run (defaults to 100 ps). The appropriate value for this parameter depends on the speed of diffusive motion of the components of the system being simulated. This can be determined by examining the MSD-time, and $\log_{10}(\text{MSD})-\log_{10}(\text{time})$ plots produced by calculations for the system in question.
- *Time step*: Time step size employed in solving the equations of motion under an NVE ensemble.
- *Sampling*: Number of samples employed in performing averaging. This parameter does not affect dynamics.
- *Trajectory*: Number of trajectory frames saved during the molecular dynamics calculation. This parameter does not affect dynamics.
- *Subset*: One or more subsets of atoms for which MSD information will be accumulated.

3 Theoretical Background

The mean square displacement of a system of 216 argon atoms with a density of 0.68043 g/cm³ at 150K as a function of time is shown below.



This approximately linear plot indicates the presence of a fully random Brownian motion where the Einstein relation is valid for extracting diffusivity from mean square displacement:

$$D = \frac{\langle (r(t) - r(t_0))^2 \rangle}{2d(t - t_0)}$$

where the numerator is the mean squared displacement, r is the position, t the elapsed time, d the dimensionality of the simulation cell, and D the self-diffusion coefficient.

As illustrated, the computation of D is best achieved by employing the central portion of the mean square displacement from a given trajectory. This avoids the intrinsic nonlinearity present at short timescales where few collisions have occurred. (In this region, sometimes called the ballistic regime, displacement is linearly proportional to elapsed time because no collisions have yet occurred and the mean squared displacement is, therefore, more quadratic than linear.)

In addition, the final portion of the mean square displacement plot may be affected by the sample averaging scheme employed (depending on the number of steps included in each sample). Hence the *Diffusion* stage employs the central 50% of the time range in its linear regression analysis of the mean square displacement plot, as illustrated.

The raw data associated with this plot are stored in the text file, $\{stageid\}_{msd.gdt}$, where $\{stageid\}$ represents the label of the *Diffusion* stage in this particular *MedeA LAMMPS* flowchart, and may be further analyzed using any appropriate plotting or analysis software.

The *MedeA* environment will also place graphics files (in both gif and png format) for the mean square displacement data in the stage directory. These provide a convenient visual indication of diffusive behavior of the set of atoms specified in this calculation. The components of mean square displacement in the X, Y, and Z simulation cell directions are also provided in these output files, allowing for the straightforward analysis of non-isotropic diffusion.

The *Diffusion* stage reports the self-diffusion coefficient of the selected atoms based on the Einstein relation and thus relies on the presence of fully random Brownian motion where the Einstein relation is applicable. For many systems, achieving the truly random collisions necessary for Brownian diffusion may require substantial simulation times. The smallest diffusion coefficients that can be determined using this technique will depend on the available computational resource, but as a rule of thumb, the smallest measurable diffusivities will be of the order of 10^{-7} cm²/s on most computers.

Given the Einstein relation, we can confirm the presence of Brownian diffusion through a plot of $\log_{10}(\text{MSD})$ versus $\log_{10}(t)$, (base 10 logarithms simply being chosen for ease of interpretation). The resulting plot should be linear and have a unit gradient. The *MedeA* calculation environment automatically carries out this analysis, and reports the gradient of the plot and the characteristics of the best fit line to these data in the *Job.out* and $\{stageid\}_{log10_msd.log10_t.gif}$ and png files in the *Diffusion* stage folder. A $\log_{10}(\text{MSD})$ versus $\log_{10}(t)$ plot, for the argon system described above, is provided below:

