

Electronics

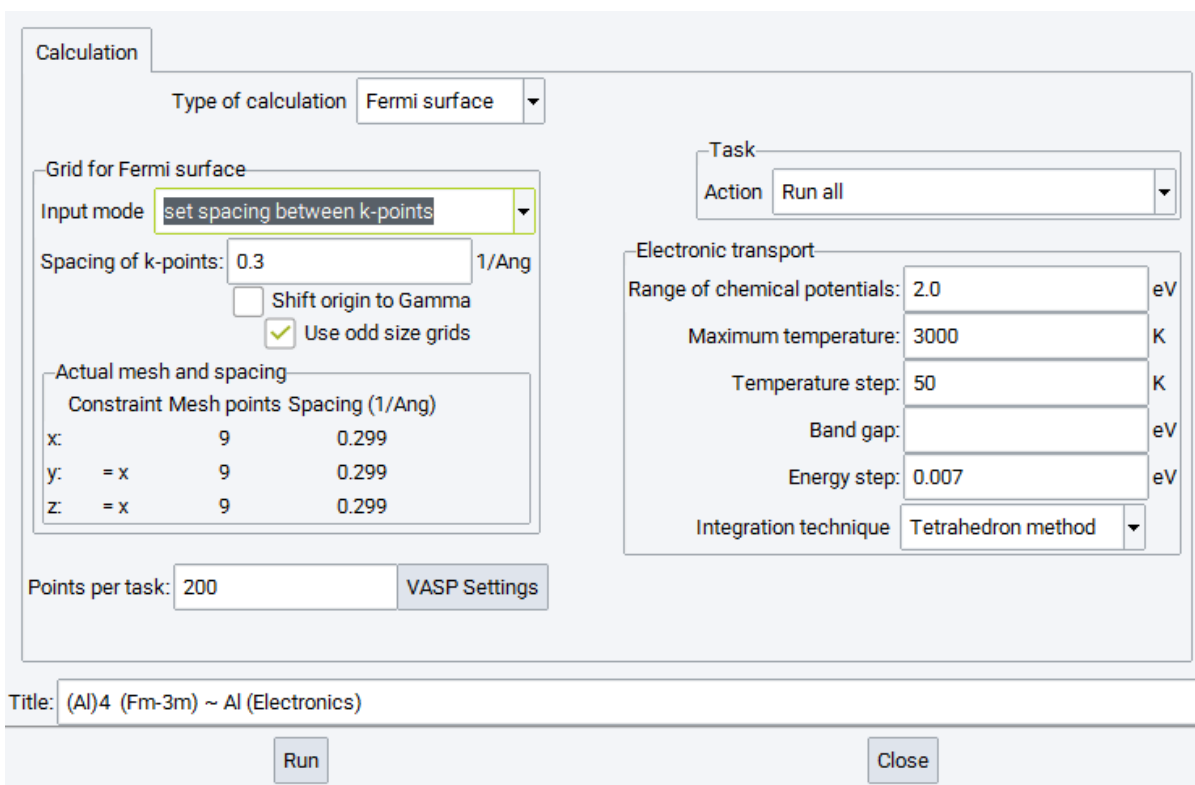
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Electronics gives you access to the so-called low-energy excitations. Under this term physicists subsume all those electronic properties, which involve electronic states in a narrow energy range around the Fermi energy, usually within a few $k_B T$. Of course, a lot of information can be deduced from the electronic states at the Fermi energy itself, as, e.g. from the Fermi surface. Yet, including electronic states nearby allows investigating electronic transport.

Specifically, *Electronics* allows you to calculate the electronic energies as a function of the **k**-vector on a regular 3-dimensional (3D) mesh spanning the Brillouin zone. You can then display 3-dimensional isoenergy surfaces of the band structure and compute effective masses and band velocities on a given surface. In particular, for metals *Electronics* yields the Fermi surface. In addition, an estimate of effective electron masses can be made (precise effective masses are obtained via the “Electronic Mass” stage in a Flowchart).

To run *Electronics* jobs, select **Electronics** from the **Tools** menu, click the new menu entry **Electronics** in the *MedeA* main menu and select **Run**.



Calculation

Type of calculation: Fermi surface

Grid for Fermi surface

Input mode: set spacing between k-points

Spacing of k-points: 0.3 1/Ang

Shift origin to Gamma

Use odd size grids

Actual mesh and spacing

	Constraint	Mesh points	Spacing (1/Ang)
x:	= x	9	0.299
y:	= x	9	0.299
z:	= x	9	0.299

Points per task: 200 **VASP Settings**

Task: Action Run all

Electronic transport

Range of chemical potentials: 2.0 eV

Maximum temperature: 3000 K

Temperature step: 50 K

Band gap: eV

Energy step: 0.007 eV

Integration technique: Tetrahedron method

Title: (Al)4 (Fm-3m) ~ Al (Electronics)

Run **Close**

The **Run** interface is similar to what you know from the SCF panel of the VASP interfaces. Select a rather fine mesh of k-points, with a **Spacing of k-points** such as 0.15 \AA^{-1} (default 0.3 \AA^{-1}), the number of points

to be used per VASP task (default **Points per task** = 25), and select further **Vasp Settings** to set additional VASP parameters. The module will determine a 3-dimensional **k**-point mesh for the Brillouin zone of the current structure (periodic lattice) and run a number of Vasp tasks to yield the electronic energies on the **k**-points of the 3D mesh for later visualization.

In addition, *Electronics* allows calculating electronic transport properties using Boltzmann theory as implemented in the BoltzTraP [1] code. This includes particularly the electronic conductivity, the thermoelectric power, the electronic contribution to the thermal conductivity, and the electronic specific heat. These quantities can be calculated for a set of temperatures and a range of chemical potentials, the latter mimicking the effect of doping within a rigid band scheme. Finally, for semiconductors and insulators the code allows adjusting the optical band gap to the desired value (the latter is also known as the scissors operator approach).

To this end, the right part of the **Run Electronics** interface offers fields to specify the **Range of chemical potentials** (extending from $E_F - 0.15$ eV to $E_F + 0.15$ eV in the example above), the **Maximum temperature**, the **Temperature step**, and the optical **Band gap** in case this should be adapted in the case of semiconductors and insulators. The **Energy step** field allows you to customize the energy increment for numerical integrations, which can be useful to tune the accuracy of the integration algorithm. Finally, the interface offers a choice between the **Histogram method** and the linear **Tetrahedron method** for Brillouin zone integration, the latter of which is recommended.

Care should be taken specifying the **k**-point mesh. While of course, the quality of the results increases with the resolution of the grid, the computational time of the background BoltzTraP calculations may need an hour (or much more for larger unit cells) for meshes with a spacing of the order of 0.1 \AA^{-1} (as selected for the results shown below).

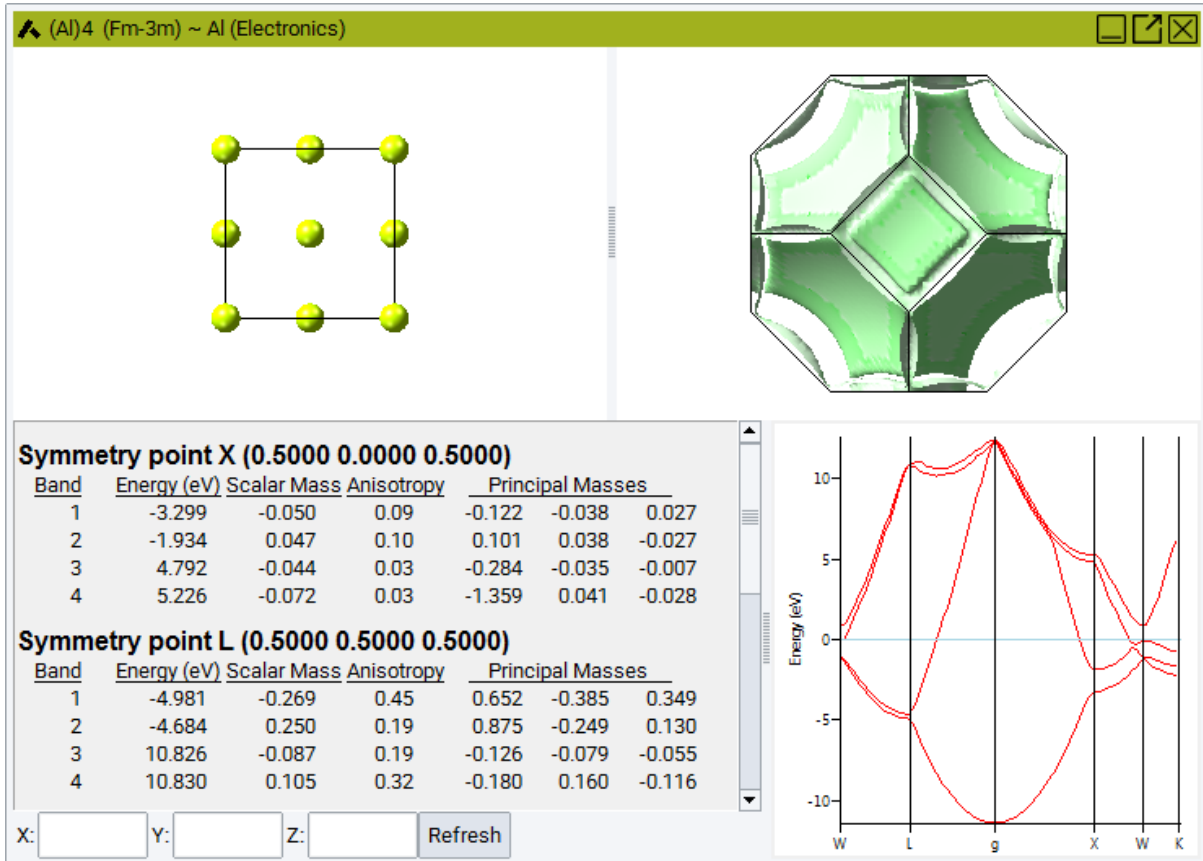
Finally, the Task frame allows specifying the particular **Action** to be taken. Here a choice can be made between **Run all**, **Calculate Fermi surface only**, and **Recalculate electronic transport**. The latter option is useful if the BoltzTraP calculation should be redone with a new range of chemical potentials or a new set of temperatures.

Visualization of the calculated results distinguishes between the isoelectronic surfaces and the electronic transport properties. To visualize an isoenergy surface, choose **Fermi Surface** from the **Electronics** menu and select results from a completed job.

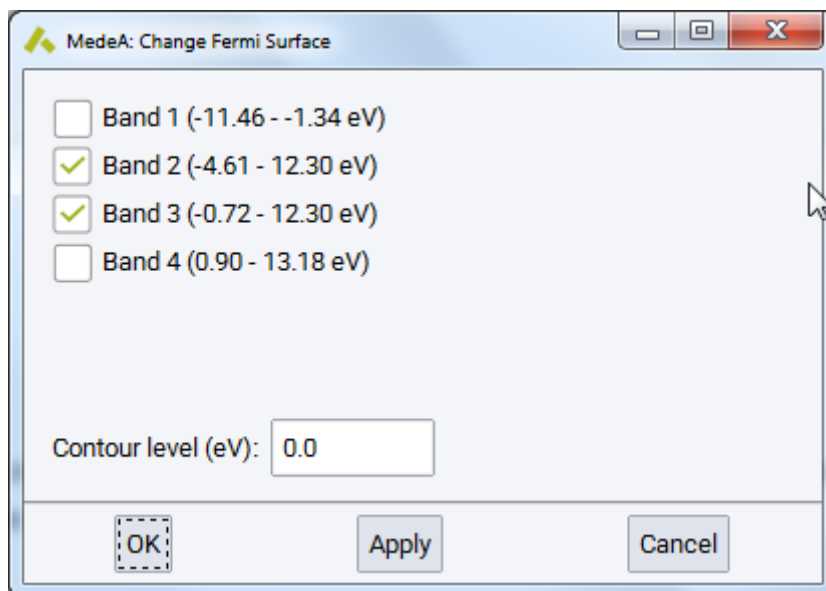
1 Fermi Surface

The latter will open a new window, which splits into four parts: The top row shows the structure (left) and the reciprocal cell (right). For metals the reciprocal cell window displays also the Fermi surface. The bottom row displays numerical results per **k**-point and band (left) and the band structure plot (right). Note that the latter comprises only a limited number of bands within a rather narrow energy window around the Fermi energy. In addition, this band structure arises from projecting the electronic energies as calculated on the pre-specified regular **k**-point grid to the so-called high-symmetry lines. This is different from calculating the band structure directly from the VASP interface, which invokes direct calculation of the electronic energies at the **k**-points aligned along the high-symmetry lines and thus is able to return a more accurate band structure.

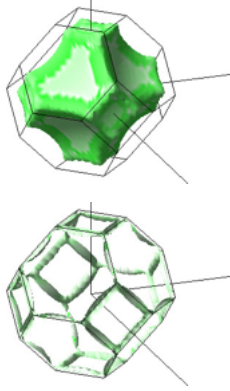
[1] Georg K H Madsen and David J Singh, "BoltzTraP. a Code for Calculating Band-Structure Dependent Quantities," Computer Physics Communications 175, no. 1 (July 2006): 67-71.



Within the Fermi Surface visualization window, the display of the isoenergy surfaces within the reciprocal cell still offers some manipulations. Of course, the reciprocal cell with the isoenergy surface can be rotated and zoomed as well-known from the real space structure.



Yet, additional options can be accessed by choosing Change the Fermi Surface from the Electronics menu. This opens a new dialog window, which allows adjusting the contour level of the isoenergy surface (relative to the Fermi energy) and selecting particular bands for the display. To facilitate selection, the dialog reports the highest and lowest energy for each band. As a default, the contour level is set to zero and all bands straddling the Fermi energy are included. Hence, for semiconductors and insulators, no surfaces are displayed by default. For aluminum, the example already shown above, the Fermi surfaces of the two bands at the Fermi energy are displayed in the figures below.



Moving the mouse over the Fermi surface graph displays information on mass, velocity and speed of the **k**-point under the mouse pointer in the status bar at the bottom of the window.

Approximate Effective Masses

In the lower left part of the **Fermi Surface** visualization window, some numerical results are printed for a selected set of bands at the high-symmetry points (defining the high-symmetry lines used in the band structure plot at the lower right). They are based on the so-called effective mass tensor, which is given by

$$m_{\alpha\beta}^{-1} = \frac{\partial^2 \epsilon_n(k)}{\partial k_\alpha \partial k_\beta}$$

i.e. the curvature of a band at a particular **k**-point. The printed quantities include

- energy and scalar mass (geometric mean of the principal masses m_i , which are the eigenvalues of the effective mass tensor) multiplied by the degeneracy factor $g^{\frac{2}{3}}$

$$m = g^{\frac{2}{3}} \sqrt[3]{m_1 m_2 m_3}$$

- mass anisotropy

$$\Delta M = \sqrt{\frac{m_1}{m_2 m_3}} \quad \text{with} \quad m_1 \geq m_2 \geq m_3$$

- principal masses, *i.e.* the eigenvalues of the effective mass tensor

Note: Note that for calculating conductivity in the Drude model the *effective mass* m^* is defined as

$$m^* = \frac{3}{\sum_{\alpha} \frac{1}{m_{\alpha}}}$$

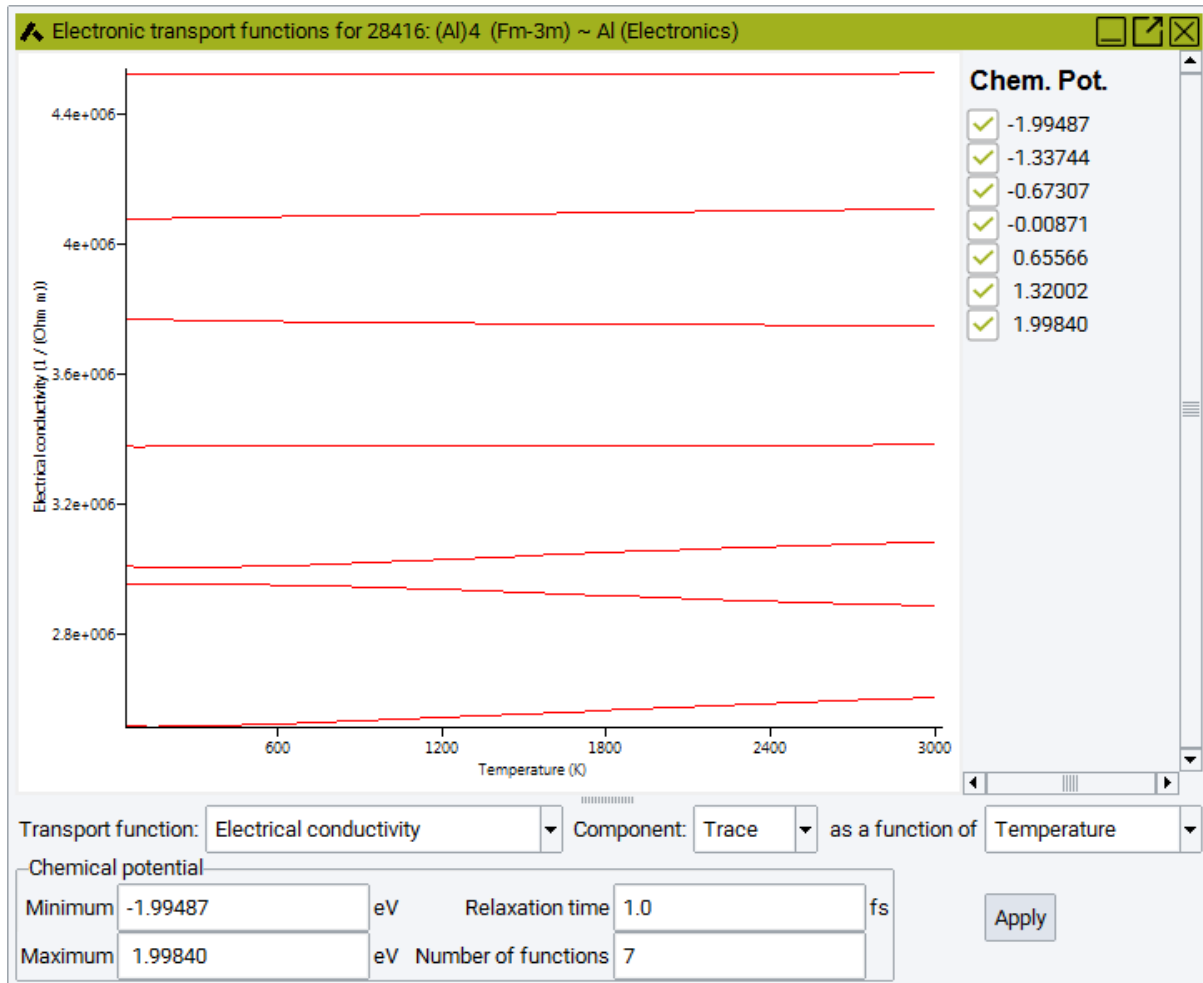
In order to print these quantities at arbitrary **k**-points, specify and (custom) that **k**-point using the three entry fields: X: ___ Y: ___ Z: ___ and confirm with **Refresh**. To restore the printing of these quantities at the high-symmetry points just blank out the three entry fields and press the **Refresh** button again.

2 Electronic Transport

To visualize the results of the electronic transport calculations as covered by the BoltzTraP code, choose **Electronic Transport** from the **Electronics** menu and select the completed job.

This will open a new window, which comprises a graphical display and several option entries and choices. Initially, the graphical display shows the trace of the electrical conductivity tensor as a function of temperature for several values of the chemical potential (in eV relative to the Fermi energy), which are displayed right to

the graph (Chem. Pot.). By dragging the mouse pointer across the various values of the chemical potential, they turn red and the respective curve is highlighted.



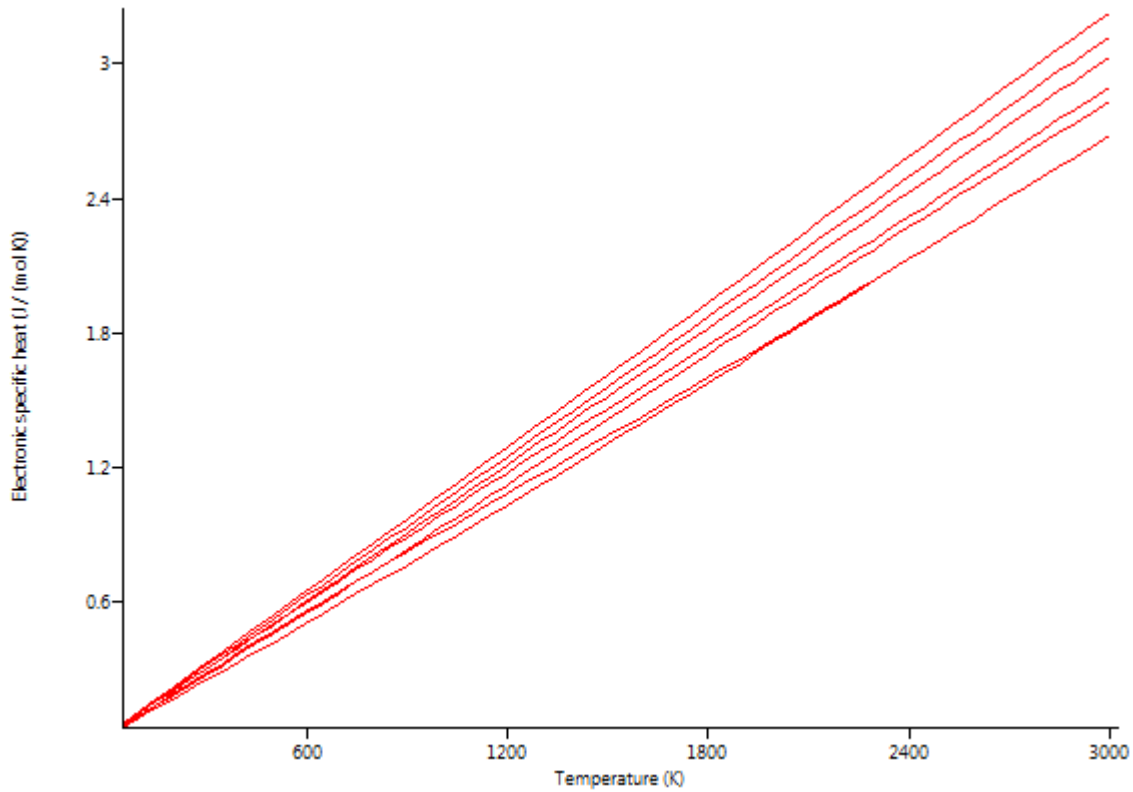
In the lower part of the window, display of the **Electrical Conductivity** can be replaced by one of the following: **Rigid band doping**, **Carrier density**, **Density of states** (at the Fermi energy), **Seebeck coefficient** (or **thermoelectric power**), **Electronic fitness function**, **Inverse transport effective mass**, **Hall coefficient**, the electronic contribution to the **Thermal conductivity**, **Electronic specific heat**, or **Pauli paramagnetic susceptibility**. In addition, the **Component** of the corresponding tensor or else its **Trace** can be selected. Finally, all these quantities can be displayed as a function of **Temperature** (at different values of the chemical potential), as a function of **Chemical Potential** (at different values of the temperature) or as a function of **Carrier density** (at different values of the temperature). Depending on this choice, **Minimum** and **Maximum** values for either the chemical potential or the temperature, as well as the **Number of functions** to be displayed can be selected.

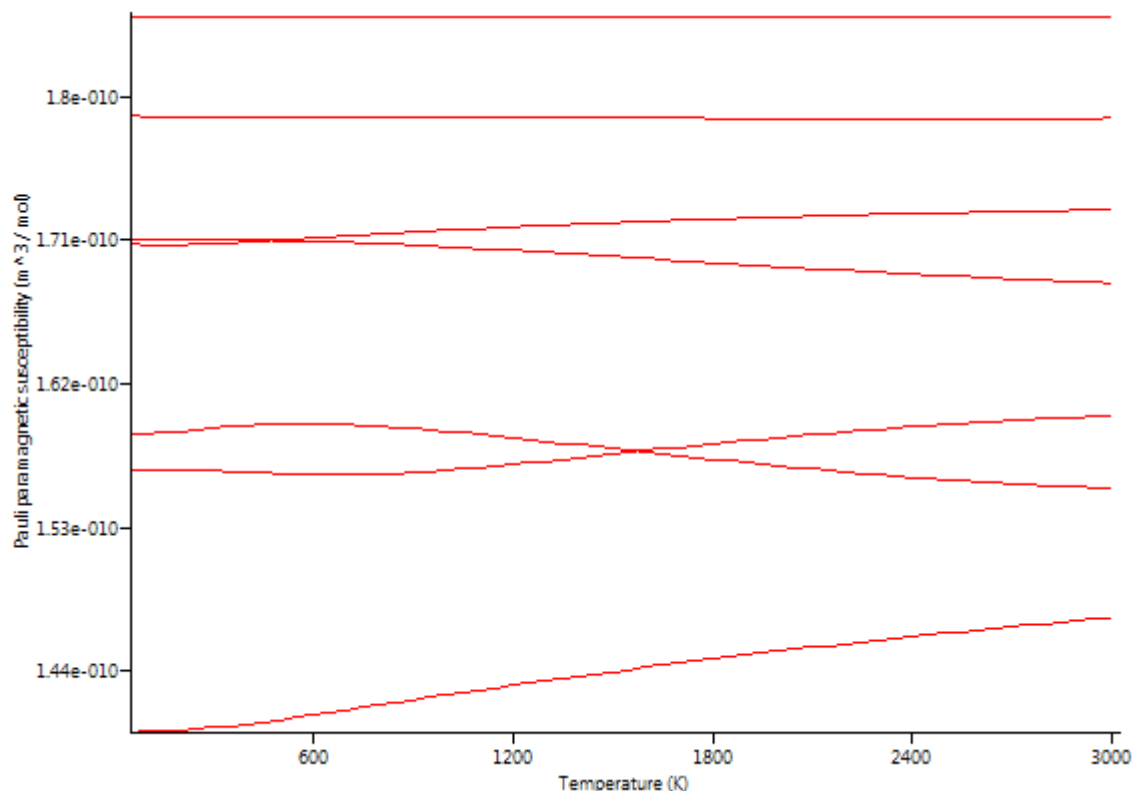
Finally, some of the quantities to be displayed still depend on the choice of the so-called **Relaxation time**, which can be set in the corresponding entry field. In this context it should be noted that BoltzTraP relies on the relaxation-time approximation, which replaces the in general **k**-vector and band dependent relaxation time by a single value, which is the same at all **k**-points and for all bands. While for some quantities as, e.g., the **Seebeck coefficient**, the so approximated relaxation time cancels out, it still enters other quantities as a linear prefactor. This applies to the **Electrical Conductivity** and the electronic contribution to the **Thermal conductivity**. In contrast, in addition to the Seebeck coefficient, **Rigid band doping**, the **Carrier density**, the **Density of states** at the Fermi energy, the **Hall coefficient**, the **Electronic specific heat**, and the **Pauli paramagnetic susceptibility** are independent of the relaxation

time.

Any change of the four input parameters grouped in the frame need to be applied either by pushing the **Apply** button, or by changing the **Transport function**, their **Component** or the x-axis definition (**as a function of**), to become effective in the graph.

As examples the figures below display the electronic specific heat (left) and the Pauli paramagnetic susceptibility of Al (right), which as expected show the almost linear dependence on temperature and the nearly temperature-independent behavior, respectively.

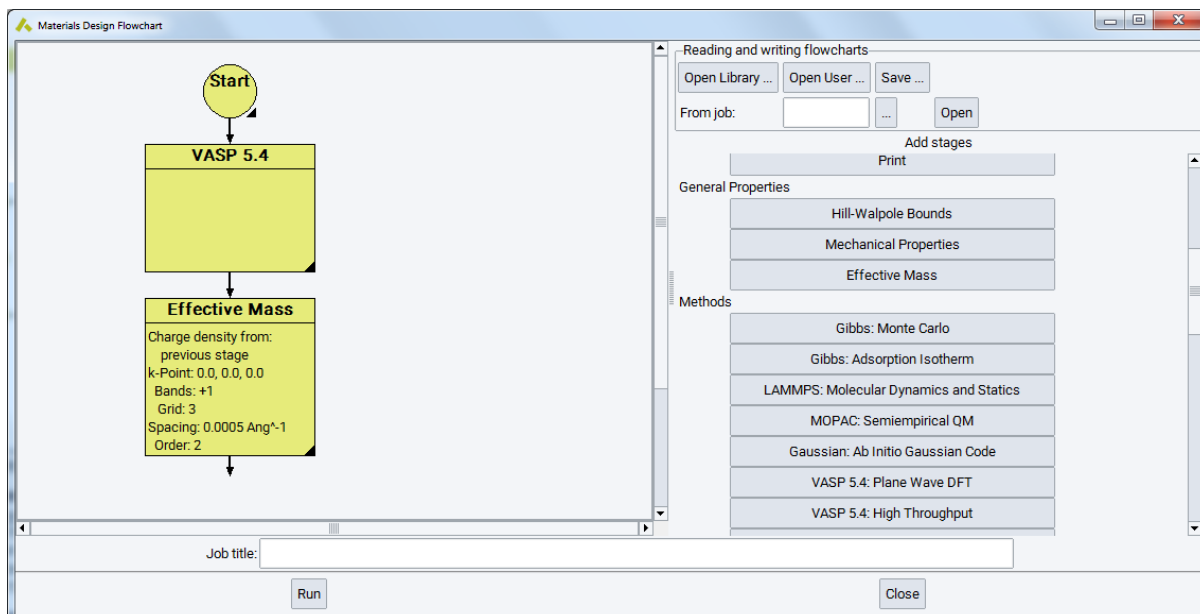




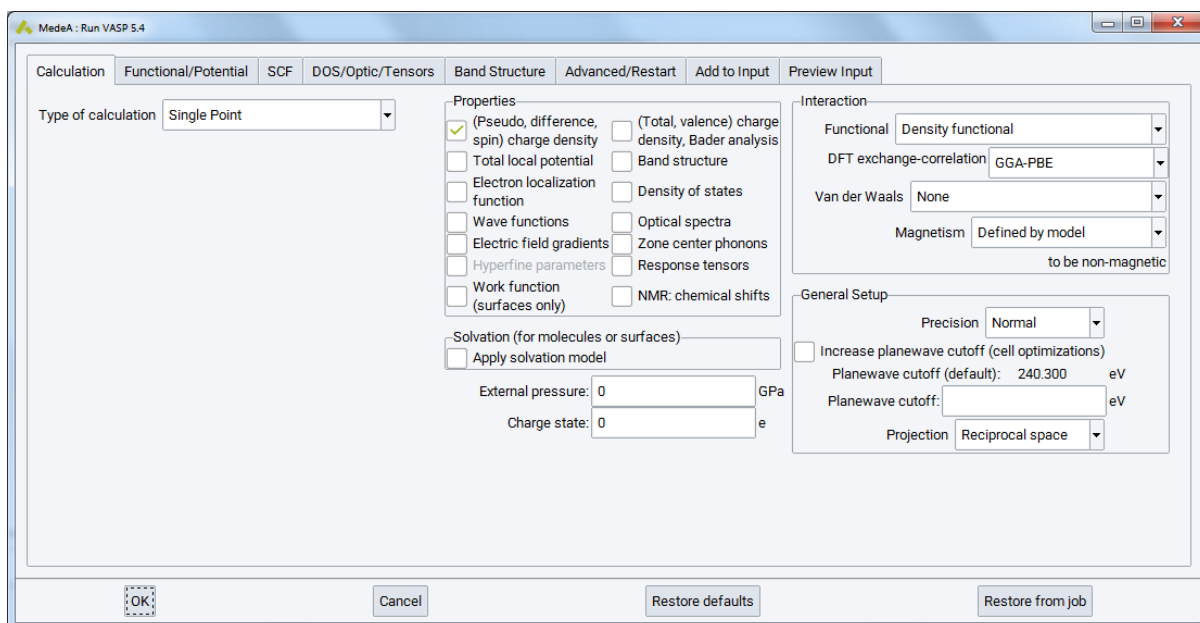
3 Accurate Effective Masses

In addition to allowing access to the Fermi surface and the transport properties, *Electronics* provides an alternative means to compute high-accuracy effective masses, which is based on zooming into specified **k**-points and the use of a fine local **k**-mesh. The latter is a fine grid of **k**-points centered about the **k**-point of interest and usually consisting of 3x3x3, 5x5x5, or 7x7x7 points. Calculated energy states at these grid points are fed into a highly-efficient non-linear least-squares fit, from which the so-called effective mass tensor is extracted. Diagonalization of the effective mass tensor then yields the principle masses according to the formulas noted above.

This functionality can be accessed via the **Job Control** >> **New Job...** menu item. In this menu, add to the **Start** stage a VASP calculation by clicking VASP 5.4: Density Functional Theory (or any other VASP version) from the **Methods** section, and **Effective Mass** from the **General Properties** section on the right-hand side of the window. As a result, the following Flowchart is obtained.



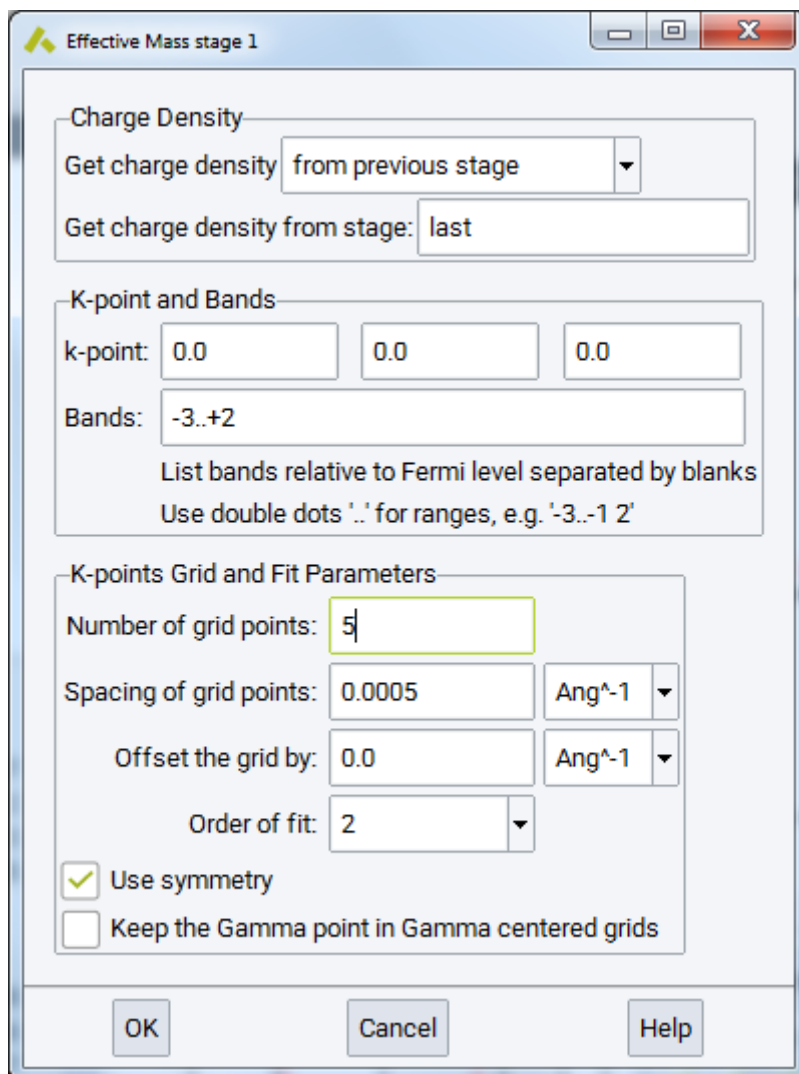
Still, the single stages need some attention. As described before, double-clicking the VASP 5.4 stage allows adapting the parameters of the VASP calculation. Two points are particularly noteworthy. First, click the box (Pseudo, difference, spin) charge density as indicated in the following figure since the subsequent Effective Mass stage will need the charge density as input.



Second, the calculation of correct effective masses requires a very high accuracy already at this stage of the calculation. For this reason, make sure that the **k**-point mesh is fine enough and do not go below normal precision or the default plane-wave cutoff. It is proposed to adapt these important parameters until converged results for the effective masses are obtained. Here, the *MedeA Automated Convergence* tool can be helpful.

In the same way as for the VASP 5.4 stage, double-clicking the Effective Mass stage opens a new dialog window as is shown below, which can be used to access the full functionality of the Effective Mass calculation. In particular, the **k**-point, at which the effective mass(es) will be calculated, has to be selected as well as the range of Bands to be included in the calculation. Furthermore, the Grid size can be specified (e.g., 5x5x5 as in the example shown below) and the Grid spacing of the local grid. For the Order of fit, while a 2nd order fit will suffice for most bands, even up to 4th order fits can be performed. Finally, the dialog allows specifying whether to use symmetry, whether to keep the Gamma point in Gamma centered grids, and

whether to **Offset the grid by** a certain distance in reciprocal Angstrom units away from its default centering about the k-point specified before.



The results of the analysis of the electronic bands are written to the file *Job.out*. There, for each band in the requested range RMS (root mean square) values for the non-linear least-squares fit are given together with the fitted band energy, the effective mass tensor, and the resulting principal masses. Finally, most of these data are summarized at the end in the form of a small table for better readability. The calculation of accurate effective masses requires well converged electronic bands and well adapted local **k**-point grids. For this reason, please check your results with respect to an optimal setting of all calculation parameters.